Unit 18: Training Data vs. Test Data

Case Study: Building a Model that is Good at Predicting Approval for the President's Foreign Policy with Age, Sex, and Political Affiliation *with New Data*

Suppose we work at a political advertising agency. Rather than seek to **understand the relationship** between approval for the president's foreign policy with sex, age, and political affiliation, we would like build a model that will give us the **best predictions** for adults living in the U.S. in which we *don't know what they think about the president's foreign policy*.

We can assume that this agency has the age, sex, political affiliation, and address of all registered voters in the state. So one goal that this political advertising agency might have is to use this data to make predictions about whether a given person that lives at a particular house approves of the president's foreign policy. They could then use that information to decide whether to mail political advertising pamphplets to this address.

Python Libraries and Packages

Python libraries:

```
statsmodels.api, statsmodels.formula.api, scikit-learn
```

If you need to install these on your computer enter the following commands from a terminal or anaconda window:

```
conda install scikit-learn
conda install -c conda-forge statsmodels
```

Imports

In [1]:
```
import pandas as pd
import numpy as np
import seaborn as sns
import matplotlib.pyplot as plt

import statsmodels.api as sm
import statsmodels.formula.api as smf
```

1. Different Goals for Building a Regression Model

See Unit 18 slides (section 1)

Read the body dimensions dataset.

In [2]:
```
df=pd.read_csv('bdims.csv')
df.head()
```

Out[2]:

	biacromial_diameter	pelvic_breadth	bitrochanteric_diameter	chest_depth	chest_diameter	elbo
0	42.9	26.0	31.5	17.7	28.0	
1	43.7	28.5	33.5	16.9	30.8	
2	40.1	28.2	33.3	20.9	31.7	
3	44.3	29.9	34.0	18.4	28.2	
4	42.5	29.9	34.0	21.5	29.4	

5 rows × 26 columns

In [3]:
```
df.columns
```

Out[3]:
```
Index(['biacromial_diameter', 'pelvic_breadth', 'bitrochanteric_diameter',
       'chest_depth', 'chest_diameter', 'elbow_diameter', 'wrist_diameter',
       'knee_diameter', 'ankle_diameter', 'shoulder_girth', 'chest_girth',
       'waist_girth', 'navel_girth', 'hip_girth', 'thigh_girth', 'bicep_girt
h',
       'forearm_girth', 'knee_diameter.1', 'calf_girth', 'ankle_girth',
       'wrist_girth', 'age', 'weight', 'height', 'sex', 'age_group'],
      dtype='object')
```

In [4]:
```
df[['bicep_girth', 'age', 'sex', 'weight', 'height']]
```

Out[4]:

	bicep_girth	age	sex	weight	height
0	32.5	21	Male	65.6	174.0
1	34.4	23	Male	71.8	175.3
2	33.4	28	Male	80.7	193.5
3	31.0	23	Male	72.6	186.5
4	32.0	22	Male	78.8	187.2
...	...	...	...	...	...
482	30.3	29	Female	71.8	176.5
483	30.1	21	Female	55.5	164.4
484	27.4	33	Female	48.6	160.7
485	30.6	33	Female	66.4	174.0
486	33.2	38	Female	67.3	163.8

487 rows × 5 columns

In [5]:

```
results=smf.ols('bicep_girth~age+sex+weight+height', data=df).fit()
results.summary()
```

Out[5]:

OLS Regression Results

Dep. Variable:	bicep_girth	**R-squared:**	0.831
Model:	OLS	**Adj. R-squared:**	0.829
Method:	Least Squares	**F-statistic:**	590.9
Date:	Wed, 21 Apr 2021	**Prob (F-statistic):**	2.94e-184
Time:	22:52:06	**Log-Likelihood:**	-963.88
No. Observations:	487	**AIC:**	1938.
Df Residuals:	482	**BIC:**	1959.
Df Model:	4		
Covariance Type:	nonrobust		

	coef	**std err**	**t**	**P>|t|**	**[0.025**	**0.975]**
Intercept	31.4253	2.032	15.465	0.000	27.432	35.418
sex[T.Male]	3.4235	0.235	14.590	0.000	2.962	3.885
age	-0.0132	0.009	-1.547	0.123	-0.030	0.004
weight	0.2475	0.009	26.789	0.000	0.229	0.266
height	-0.1088	0.013	-8.129	0.000	-0.135	-0.083

Omnibus:	13.978	**Durbin-Watson:**	1.993
Prob(Omnibus):	0.001	**Jarque-Bera (JB):**	15.394
Skew:	0.347	**Prob(JB):**	0.000454
Kurtosis:	3.526	**Cond. No.**	4.78e+03

Notes:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
[2] The condition number is large, 4.78e+03. This might indicate that there are
strong multicollinearity or other numerical problems.

In [6]:
```
results=smf.ols('bicep_girth~sex+weight+height', data=df).fit()
results.summary()
```

Out[6]:

OLS Regression Results

Dep. Variable:	bicep_girth	**R-squared:**	0.830
Model:	OLS	**Adj. R-squared:**	0.829
Method:	Least Squares	**F-statistic:**	784.7
Date:	Wed, 21 Apr 2021	**Prob (F-statistic):**	3.19e-185
Time:	22:52:06	**Log-Likelihood:**	-965.09
No. Observations:	487	**AIC:**	1938.
Df Residuals:	483	**BIC:**	1955.
Df Model:	3		
Covariance Type:	nonrobust		

	coef	**std err**	**t**	**P>|t|**	**[0.025**	**0.975]**
Intercept	30.7279	1.984	15.486	0.000	26.829	34.627
sex[T.Male]	3.3844	0.234	14.487	0.000	2.925	3.843
weight	0.2449	0.009	26.922	0.000	0.227	0.263
height	-0.1060	0.013	-7.980	0.000	-0.132	-0.080

Omnibus:	14.566	**Durbin-Watson:**	1.991
Prob(Omnibus):	0.001	**Jarque-Bera (JB):**	16.497
Skew:	0.345	**Prob(JB):**	0.000262
Kurtosis:	3.581	**Cond. No.**	4.60e+03

Notes:
[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
[2] The condition number is large, 4.6e+03. This might indicate that there are
strong multicollinearity or other numerical problems.

2. Problem with Overfitting a Regression Model

See Unit 18 slides (section 2)

3. Training vs. Test Data

See Unit 18 slides (section 3)

4. Case Study: Building a Model that is Good at Predicting Approval for the President's Foreign Policy with Age, Sex, and Political Affiliation *with New Data*

Problem Statement: Suppose we work at a political advertising agency. Rather than seek to **understand the relationship** between approval for the president's foreign policy with sex, age, and political affiliation, we would like build a model that will give us the **best predictions** for adults living in the U.S. in which we *don't know what they think about the president's foreign policy*.

We can assume that this agency has the age, sex, political affiliation, and address of all registered voters in the state. So one goal that this political advertising agency might have is to use this data to make predictions about whether a given person that lives at a particular house approves of the president's foreign policy. They could then use that information to decide whether to mail political advertising pamphlets to this address.

4.1 Data Preliminaries

We will be using *a portion* of our 2017 random sample Pew dataset to train a logistic regression model that predicts the probability that an adult living in the U.S. supported the president's foreign policy given sex, age, and political affiliation.

Loading the dataset

In [7]:
```
missing_values = ["NaN", "nan", "Don't know/Refused (VOL.)"]
df = pd.read_csv('Feb17public.csv',
                 na_values=missing_values)[['age', 'sex', \
                                             'q5cf1', 'party']]
df.head()
```

Out[7]:

	age	sex	q5cf1	party
0	80.0	Female	NaN	Independent
1	70.0	Female	Disapprove	Democrat
2	69.0	Female	Disapprove	Independent
3	50.0	Male	NaN	Republican
4	70.0	Female	Disapprove	Democrat

Dropping missing values

Let's first drop the rows in this dataset with missing values.

In [8]:
```
df = df.dropna()
df.head()
```

Out[8]:

	age	sex	q5cf1	party
1	70.0	Female	Disapprove	Democrat
2	69.0	Female	Disapprove	Independent
4	70.0	Female	Disapprove	Democrat
6	89.0	Female	Disapprove	Independent
7	92.0	Female	Approve	Republican

Size of the dataset.

In [9]:
```
n=df.shape[0]
n
```

Out[9]: 679

Creating a 0/1 response variable value for the logistic regression model where:

- approve =1 and
- disapprove =0.

In [10]:
```
df['y'] = df['q5cf1'].map({'Disapprove':0,'Approve':1})
df.head()
```

Out[10]:

	age	sex	q5cf1	party	y
1	70.0	Female	Disapprove	Democrat	0
2	69.0	Female	Disapprove	Independent	0
4	70.0	Female	Disapprove	Democrat	0
6	89.0	Female	Disapprove	Independent	0
7	92.0	Female	Approve	Republican	1

4.2 Creating the Training and Test Dataset

Next, we split the data into the:

- **training dataset**: where we randomly select 80% of observations from Pew dataset and the
- **test data set**: comprised of the remaining 20% of observations from Pew dataset.

It's usually best to have your training dataset have much more observations than your test dataset!

We use the **train_test_split()** function from the **sklearn.model_selection** package to do this. The parameters for this function are:

- the dataframe we wish to randomly split into a training dataset and a test dataset
- the **test_size**= the percent of the dataset we would like to be allocated to the test dataset
- we an also supply a **random_state** number.

In [11]:
```
from sklearn.model_selection import train_test_split

df_train, df_test = train_test_split(df,
                                     test_size=0.20,
                                     random_state=123)
```

Let's inspect the newly created training dataset.

In [12]:
```
df_train
```

Out[12]:

	age	sex	q5cf1	party	y
725	39.0	Female	Disapprove	Democrat	0
836	67.0	Female	Disapprove	Democrat	0
961	51.0	Male	Disapprove	Democrat	0
348	72.0	Male	Approve	Republican	1
1025	61.0	Female	Disapprove	Democrat	0
...	...	...	...	...	...
205	90.0	Female	Approve	Republican	1
693	20.0	Male	Approve	Independent	1
838	68.0	Male	Approve	Republican	1
791	56.0	Male	Disapprove	Independent	0
1115	45.0	Male	Approve	Independent	1

543 rows × 5 columns

We can double check that this training dataset contains about 80% of the observations from df.

In [13]:
```
df_train.shape[0]/df.shape[0]
```

Out[13]: 0.7997054491899853

Let's inspect this new test dataset.

In [14]:
```
df_test
```

Out[14]:

	age	sex	q5cf1	party	y
337	79.0	Female	Approve	Republican	1
424	30.0	Female	Disapprove	Independent	0
751	46.0	Male	Disapprove	Independent	0
1423	77.0	Male	Disapprove	Democrat	0
1367	58.0	Male	Approve	Independent	1
...	...	...	...	...	...
872	42.0	Female	Approve	Republican	1
915	52.0	Male	Disapprove	Democrat	0
535	22.0	Male	Disapprove	Independent	0
1075	69.0	Female	Disapprove	Democrat	0
933	74.0	Male	Disapprove	Independent	0

136 rows × 5 columns

We can double check that this test dataset contains about 20% of the observations from df.

In [15]:
```
df_test.shape[0]/df.shape[0]
```

Out[15]: 0.20029455081001474

4.3. Fit (ie. *train*) the model to *training data*.

Next we will **train** our logistic regression model with the **training dataset** only.

In [16]:
```
pewmod = smf.logit('y ~ party + age + sex',\
    data=df_train).fit()
pewmod.summary()
```

```
Optimization terminated successfully.
         Current function value: 0.402672
         Iterations 7
```

Out[16]:

Logit Regression Results

Dep. Variable:	y	**No. Observations:**	543
Model:	Logit	**Df Residuals:**	536
Method:	MLE	**Df Model:**	6
Date:	Wed, 21 Apr 2021	**Pseudo R-squ.:**	0.3899
Time:	22:52:06	**Log-Likelihood:**	-218.65
converged:	True	**LL-Null:**	-358.39
Covariance Type:	nonrobust	**LLR p-value:**	2.035e-57

	coef	**std err**	**z**	**P>|z|**	**[0.025**	**0.975]**
Intercept	-4.6644	0.535	-8.719	0.000	-5.713	-3.616
party[T.Independent]	2.1964	0.352	6.232	0.000	1.506	2.887
party[T.No preference (VOL.)]	2.7477	0.722	3.805	0.000	1.332	4.163
party[T.Other party (VOL.)]	4.0648	1.230	3.306	0.001	1.655	6.475
party[T.Republican]	4.4606	0.388	11.498	0.000	3.700	5.221
sex[T.Male]	0.9140	0.252	3.633	0.000	0.421	1.407
age	0.0271	0.007	3.840	0.000	0.013	0.041

4.4 *Test* the model's predictive accuracy with the *test dataset*.

Finally, in order to get an idea as to how well our trained logistic regression model with perform with new data (that was not factored in to the optimal selection of $\hat{\beta}_0, \hat{\beta}_1, ..., \hat{\beta}_p$) we will calculate various metric that assess the predictive performance of our model with the **test dataset** including the:

- ROC
- AUC
- sensitivity and specificity for a few selected predictive probability thresholds.

4.4.1 First, get the predictive probabilities of the *test dataset* with this trained model.

The predict function uses the fitted model to extract any exogenous variables it needs from the test data. We do not have to specify which variables. We just provide the whole test data frame. Compare the following two code cells and results.

In [17]:
```
# predictive probabilities - explicit method
phat_test = pewmod.predict(exog=df_test[['age', 'sex', 'party']])
phat_test.head(10)
```

Out[17]:
```
337     0.874386
424     0.160607
751     0.424221
1423    0.159691
1367    0.505054
440     0.079614
801     0.850883
1279    0.890355
187     0.082286
342     0.057777
dtype: float64
```

In [18]:
```
# predictive probabilities - implicit method
phat_test = pewmod.predict(exog=df_test)
phat_test.head(10)
```

Out[18]:
```
337     0.874386
424     0.160607
751     0.424221
1423    0.159691
1367    0.505054
440     0.079614
801     0.850883
1279    0.890355
187     0.082286
342     0.057777
dtype: float64
```

```
In [19]: df_test['phat_test']=phat_test
         df_test
```

```
<ipython-input-19-c185c916a8e2>:1: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/s
table/user_guide/indexing.html#returning-a-view-versus-a-copy
  df_test['phat_test']=phat_test
```

Out[19]:

	age	sex	q5cf1	party	y	phat_test
337	79.0	Female	Approve	Republican	1	0.874386
424	30.0	Female	Disapprove	Independent	0	0.160607
751	46.0	Male	Disapprove	Independent	0	0.424221
1423	77.0	Male	Disapprove	Democrat	0	0.159691
1367	58.0	Male	Approve	Independent	1	0.505054
...	...	...	...	...	...	...
872	42.0	Female	Approve	Republican	1	0.718312
915	52.0	Male	Disapprove	Democrat	0	0.087940
535	22.0	Male	Disapprove	Independent	0	0.277510
1075	69.0	Female	Disapprove	Democrat	0	0.057777
933	74.0	Male	Disapprove	Independent	0	0.611701

136 rows × 6 columns

4.4.2 Next, we generate the ROC curve and calculate the AUC for the *test dataset*.

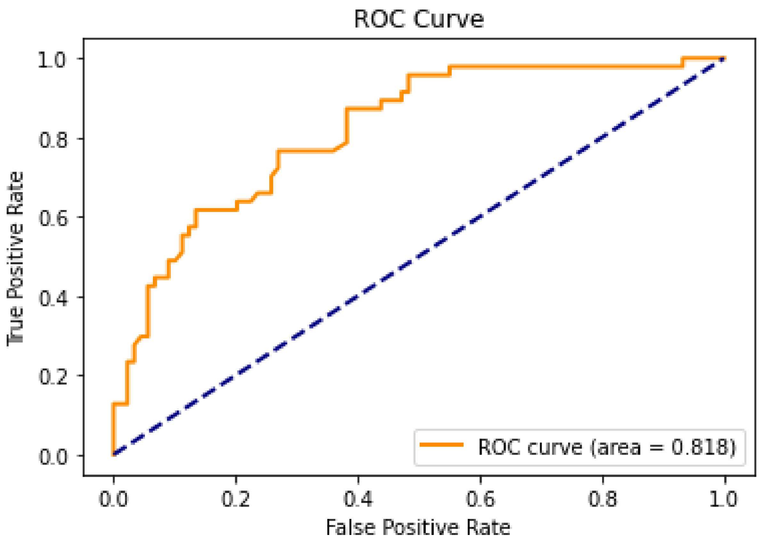
```
In [20]: from sklearn.metrics import roc_curve
         from sklearn.metrics import roc_auc_score

         fpr_pew, tpr_pew, score_pew = roc_curve(y_true=df_test['y'], y_score=df_test[
         'phat_test'])
         auc_pew = roc_auc_score(y_true=df_test['y'], y_score=df_test['phat_test'])
```

```
In [21]: def plot_roc(fpr, tpr, auc, lw=2):
             plt.plot(fpr, tpr, color='darkorange', lw=lw,
                      label='ROC curve (area = '+str(round(auc,3))+')')
             plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
             plt.xlabel('False Positive Rate')
             plt.ylabel('True Positive Rate')
             plt.title('ROC Curve')
             plt.legend(loc="lower right")
             plt.show()
```

In [22]:

```
plot_roc(fpr_pew, tpr_pew, auc_pew)
```



Interpretation:

<u>Evaluation</u>: The AUC for the **test dataset** is 0.818.

<u>What can we use it form</u>: This gives us a sense of how good our logistic regression model (which has been trained with the **training dataset**) would be at predicting the probability that an adult living in the U.S. approves of the president's foreign policy with *new data* (in which we don't know the actual answer of whether they disapprove or approve.

<u>Interpreting AUC</u>: Because the AUC is somewhat high (ie. closer to 1 than it is to 0.5), this tells us that there does exist some predictive probability threshold that gets somewhat close to giving us the ideal scenario of a model with a false positive rate of 0 and a true positive rate of 1 with new data.

4.5 Finding a "good" (FPR, TPR) combination.

Ideally, we would like to pick a predictive probability threshold that gives us a false positive rate of 0 and true positive rate of 1. However, this ROC curve shows that there does not exist a predictive probability threshold that will give us this ideal combination. So what predictive probability threshold should we choose?

Well, it depends on much a high **true positive rate** is worth to you vs. a low **false positive rate** is to you.

<u>Here's a couple options.</u>

<u>Option 1</u>: About (FPR = 0.5, TPR = 0.95)

Notice how that at a FPR of 0.5, the TPR starts to level off in the ROC curve above. By increasing the FPR any more past 0.5, we do not gain much more in the way of a better (higher) TPR. So we could choose the predictive probability threshold that gives us this combination of (FPR = 0.5, TPR = 0.95).

<u>Option 2</u>: About (FPR = 0.1, TPR = 0.6)

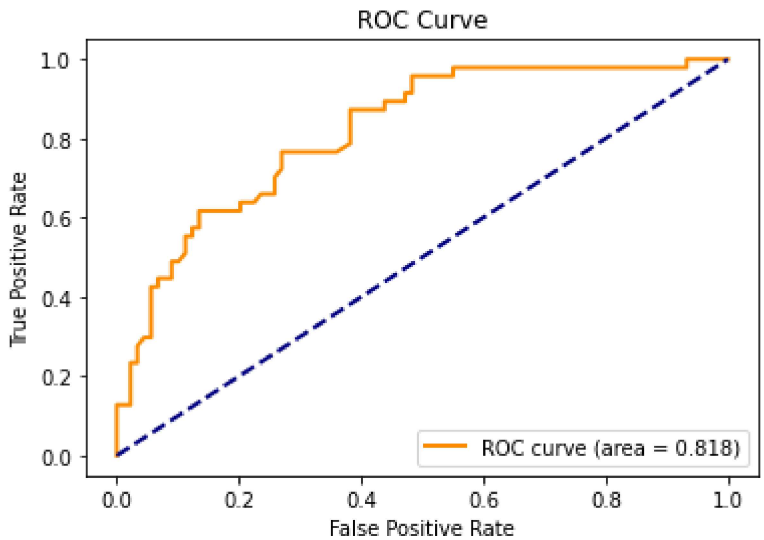
Notice how that at a TPR of 0.6, the FPR starts to level off in the ROC curve above. By decreasing the TPR any more past 0.6, we do not gain much more in the way of a better (lower) FPR. So we could choose the predictive probability threshold that gives us this combination of (FPR = 0.1, TPR = 0.6).

<u>What kind of political advertising groups would choose option 1 over option 2?</u>

<u>Political Ad Group 1</u>:

Suppose this group really values predicting as many people as possible that support the president's foreign policy (ie. are a 1 or positive). Furthermore there is no penalty for mailing ads to houses in which the homeowners don't support the policy (ie. are a 0 or negative).

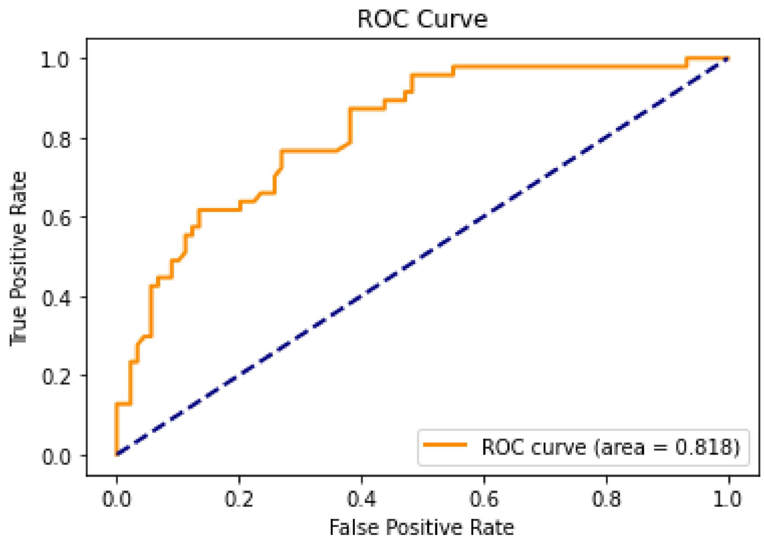
In [23]:
```
plot_roc(fpr_pew, tpr_pew, auc_pew)
```



Political Ad Group 2:

Suppose this group would *ideally* like to predict as many people as possible that support the president's foreign policy (ie. are a 1/positive), but have learned that there is a very high backfire effect when they mail ads to houses in which the homeowners don't support the policy (ie. are a 0 or negative).

```
In [24]: plot_roc(fpr_pew, tpr_pew, auc_pew)
```



4.6 Finding the predictive probability threshold that corresponds to a (FPR, TPR).

You can use this defined function below to quickly generate the fpr and tpr of a model given:

- y = the *actual* 0/1 response variable values for a given dataset
- pred_prob = the predictive probabilities for each of the observations of a given dataset
- thresh = a predictive probability threshold value

```
In [25]: from sklearn.metrics import confusion_matrix

         def tpr_fpr_thresh(y, pred_prob, thresh):
             yhat = 1*(pred_prob >= thresh)
             tn, fp, fn, tp = confusion_matrix(y_true=y, y_pred=yhat).ravel()
             tpr = tp / (fn + tp)
             fpr = fp / (fp + tn)
             return pd.DataFrame({'threshold':[thresh],
                                  'tpr':[tpr],
                                  'fpr':[fpr]})
```

For instance, the **test dataset** has a tpr = 0.6170 and a fpr = 0.1348 given a predictive probability threshold of $p_0 = 0.5$ with this logistic regression model.

```
In [26]: tpr_fpr_thresh(df_test['y'], df_test['phat_test'], 0.5)
```

Out[26]:

	threshold	tpr	fpr
0	0.5	0.617021	0.134831

Let's iterate through a series of predictive probability thresholds starting from $p_0 = 0$ and ending with $p_0 = 1$ and a step size of 0.01, to see if we can find which predictive probability threshold will give us:

- Option 1: About (FPR = 0.5, TPR = 0.95) and
- Option 2: About (FPR = 0.1, TPR = 0.6).

In [27]:
```
for thresh in np.arange(0,1,.01):
    print(tpr_fpr_thresh(df_test['y'], df_test['phat_test'], thresh))
```

```
   threshold  tpr  fpr
0        0.0  1.0  1.0
   threshold  tpr  fpr
0       0.01  1.0  1.0
   threshold       tpr       fpr
0       0.02  0.978723  0.932584
   threshold       tpr       fpr
0       0.03  0.978723  0.831461
   threshold       tpr       fpr
0       0.04  0.978723  0.786517
   threshold       tpr       fpr
0       0.05  0.978723  0.752809
   threshold       tpr       fpr
0       0.06  0.978723  0.640449
   threshold       tpr       fpr
0       0.07  0.978723  0.606742
   threshold       tpr      fpr
0       0.08  0.978723  0.58427
   threshold       tpr       fpr
0       0.09  0.978723  0.561798
   threshold       tpr       fpr
0        0.1  0.978723  0.550562
   threshold       tpr       fpr
0       0.11  0.957447  0.550562
   threshold       tpr       fpr
0       0.12  0.957447  0.539326
   threshold       tpr       fpr
0       0.13  0.957447  0.483146
   threshold      tpr       fpr
0       0.14  0.93617  0.483146
   threshold       tpr      fpr
0       0.15  0.914894  0.47191
   threshold       tpr       fpr
0       0.16  0.893617  0.460674
   threshold       tpr       fpr
0       0.17  0.893617  0.438202
   threshold      tpr       fpr
0       0.18  0.87234  0.438202
   threshold      tpr       fpr
0       0.19  0.87234  0.438202
   threshold      tpr       fpr
0        0.2  0.87234  0.404494
   threshold      tpr       fpr
0       0.21  0.87234  0.382022
   threshold      tpr       fpr
0       0.22  0.87234  0.382022
   threshold      tpr       fpr
0       0.23  0.87234  0.382022
   threshold      tpr       fpr
0       0.24  0.87234  0.382022
   threshold       tpr       fpr
0       0.25  0.851064  0.382022
   threshold       tpr       fpr
0       0.26  0.829787  0.382022
   threshold       tpr       fpr
0       0.27  0.787234  0.382022
   threshold       tpr       fpr
```

```
0       0.28  0.765957  0.359551
   threshold       tpr       fpr
0       0.29  0.765957  0.337079
   threshold       tpr       fpr
0        0.3  0.765957  0.337079
   threshold       tpr       fpr
0       0.31  0.765957  0.325843
   threshold       tpr       fpr
0       0.32  0.765957  0.314607
   threshold       tpr       fpr
0       0.33  0.765957  0.314607
   threshold       tpr       fpr
0       0.34  0.765957  0.292135
   threshold       tpr       fpr
0       0.35  0.723404  0.269663
   threshold       tpr       fpr
0       0.36  0.723404  0.269663
   threshold       tpr       fpr
0       0.37  0.659574  0.258427
   threshold       tpr       fpr
0       0.38  0.659574  0.235955
   threshold       tpr       fpr
0       0.39  0.638298  0.213483
   threshold       tpr       fpr
0        0.4  0.617021  0.191011
   threshold       tpr       fpr
0       0.41  0.617021  0.179775
   threshold       tpr       fpr
0       0.42  0.617021  0.179775
   threshold       tpr       fpr
0       0.43  0.617021  0.168539
   threshold       tpr       fpr
0       0.44  0.617021  0.168539
   threshold       tpr       fpr
0       0.45  0.617021  0.157303
   threshold       tpr       fpr
0       0.46  0.617021  0.146067
   threshold       tpr       fpr
0       0.47  0.617021  0.146067
   threshold       tpr       fpr
0       0.48  0.617021  0.134831
   threshold       tpr       fpr
0       0.49  0.617021  0.134831
   threshold       tpr       fpr
0        0.5  0.617021  0.134831
   threshold       tpr       fpr
0       0.51  0.574468  0.134831
   threshold       tpr       fpr
0       0.52  0.574468  0.123596
   threshold       tpr       fpr
0       0.53  0.574468  0.123596
   threshold       tpr       fpr
0       0.54  0.574468  0.123596
   threshold       tpr       fpr
0       0.55  0.574468  0.123596
   threshold       tpr       fpr
0       0.56  0.574468  0.123596
```

```
   threshold       tpr       fpr
0       0.57  0.574468  0.123596
   threshold       tpr      fpr
0       0.58  0.553191  0.11236
   threshold       tpr      fpr
0       0.59  0.531915  0.11236
   threshold       tpr      fpr
0        0.6  0.510638  0.11236
   threshold       tpr      fpr
0       0.61  0.510638  0.11236
   threshold       tpr       fpr
0       0.62  0.489362  0.089888
   threshold       tpr       fpr
0       0.63  0.468085  0.089888
   threshold       tpr       fpr
0       0.64  0.446809  0.089888
   threshold       tpr       fpr
0       0.65  0.446809  0.078652
   threshold       tpr       fpr
0       0.66  0.446809  0.078652
   threshold       tpr       fpr
0       0.67  0.446809  0.078652
   threshold       tpr       fpr
0       0.68  0.446809  0.078652
   threshold       tpr       fpr
0       0.69  0.446809  0.078652
   threshold       tpr       fpr
0        0.7  0.446809  0.078652
   threshold       tpr       fpr
0       0.71  0.446809  0.067416
   threshold       tpr       fpr
0       0.72  0.425532  0.067416
   threshold       tpr       fpr
0       0.73  0.425532  0.067416
   threshold       tpr       fpr
0       0.74  0.425532  0.067416
   threshold       tpr       fpr
0       0.75  0.425532  0.067416
   threshold       tpr       fpr
0       0.76  0.425532  0.067416
   threshold       tpr      fpr
0       0.77  0.425532  0.05618
   threshold       tpr      fpr
0       0.78  0.404255  0.05618
   threshold       tpr      fpr
0       0.79  0.382979  0.05618
   threshold       tpr      fpr
0        0.8  0.361702  0.05618
   threshold       tpr      fpr
0       0.81  0.319149  0.05618
   threshold       tpr      fpr
0       0.82  0.297872  0.05618
   threshold       tpr      fpr
0       0.83  0.297872  0.05618
   threshold       tpr       fpr
0       0.84  0.276596  0.033708
   threshold       tpr       fpr
```

```
0        0.85  0.255319  0.033708
   threshold       tpr       fpr
0        0.86  0.234043  0.022472
   threshold       tpr       fpr
0        0.87  0.234043  0.022472
   threshold       tpr       fpr
0        0.88  0.212766  0.022472
   threshold       tpr       fpr
0        0.89  0.170213  0.022472
   threshold      tpr       fpr
0         0.9  0.12766  0.022472
   threshold       tpr  fpr
0        0.91  0.106383  0.0
   threshold       tpr  fpr
0        0.92  0.085106  0.0
   threshold       tpr  fpr
0        0.93  0.042553  0.0
   threshold       tpr  fpr
0        0.94  0.042553  0.0
   threshold  tpr  fpr
0        0.95  0.0  0.0
   threshold  tpr  fpr
0        0.96  0.0  0.0
   threshold  tpr  fpr
0        0.97  0.0  0.0
   threshold  tpr  fpr
0        0.98  0.0  0.0
   threshold  tpr  fpr
0        0.99  0.0  0.0
```

Option 1: It looks like a predictive probability threshold of $p_0 = 0.13$ will gve us a tpr=0.957447 and a fpr=0.483146.

Option 2: It looks like a predictive probability threshold of $p_0 = 0.50$ will gve us a tpr=0.617021and a fpr=0.134831.

4.7. For Comparison

Just for comparison, let's also create a ROC curve and AUC for this logistic regression model, now using the **training dataset** instead.

4.7.1 First, get the predictive probabilities of the *training dataset* with this trained model.

In [28]:
```
# predictive probabilities - implicit method
phat_train = pewmod.predict(exog=df_train)
phat_train.head(10)
```

Out[28]:
```
725     0.026445
836     0.054892
961     0.085788
348     0.934888
1025    0.047031
251     0.044657
73      0.477928
217     0.572393
1461    0.922323
987     0.237726
dtype: float64
```

In [29]:
```
df_train['phat_train']=phat_train
df_train
```

```
<ipython-input-29-1a816231d49d>:1: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame.
Try using .loc[row_indexer,col_indexer] = value instead

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/s
table/user_guide/indexing.html#returning-a-view-versus-a-copy
  df_train['phat_train']=phat_train
```

Out[29]:

	age	sex	q5cf1	party	y	phat_train
725	39.0	Female	Disapprove	Democrat	0	0.026445
836	67.0	Female	Disapprove	Democrat	0	0.054892
961	51.0	Male	Disapprove	Democrat	0	0.085788
348	72.0	Male	Approve	Republican	1	0.934888
1025	61.0	Female	Disapprove	Democrat	0	0.047031
...	...	...	...	...	...	...
205	90.0	Female	Approve	Republican	1	0.903685
693	20.0	Male	Approve	Independent	1	0.266759
838	68.0	Male	Approve	Republican	1	0.927960
791	56.0	Male	Disapprove	Independent	0	0.491485
1115	45.0	Male	Approve	Independent	1	0.417605

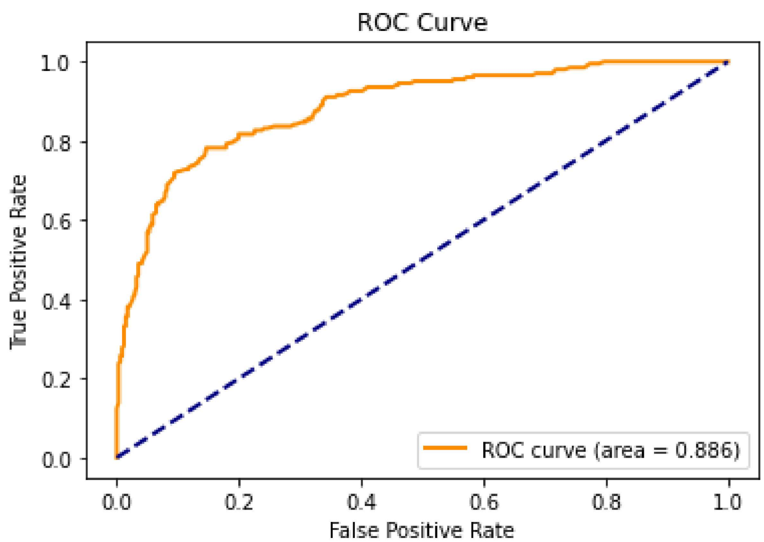
543 rows × 6 columns

4.4.2 Next, we generate the ROC curve and calculate the AUC for the *training dataset*.

In [30]:
```
from sklearn.metrics import roc_curve
from sklearn.metrics import roc_auc_score

fpr_pew, tpr_pew, score_pew = roc_curve(y_true=df_train['y'], y_score=df_train
['phat_train'])
auc_pew = roc_auc_score(y_true=df_train['y'], y_score=df_train['phat_train'])
```

In [31]:
```
plot_roc(fpr_pew, tpr_pew, auc_pew)
```



Interpretation:

Evaluation: The AUC for the **training dataset** 0.886, which is higher than it was for the test dataset (ie. AUC = 0.818).!

However, this is to be expected! We would expect to get better predictions from the **training dataset** that we specifically used to pick the values of $\hat{\beta}_0, \hat{\beta}_1, \ldots, \hat{\beta}_p$ that would fit the **training dataset** the most.

However, using this AUC of 0.886 to assess how well this model would be at predicting the probability that an adult living in the U.S. supports the president's foreign policy **for new data** would be misleading.

It is much more likely that this model would be slightly worse (with an AUC=0.818) at predicting the probability that an adult living in the U.S. supports the president's foreign policy **for new data**.